RAMAKRISHNA MISSION VIDYAMANDIRA

(Residential Autonomous College affiliated to University of Calcutta)

B.A./B.Sc. SECOND SEMESTER EXAMINATION, SEPTEMBER 2020

FIRST YEAR (BATCH 2019-22)

Date : 28/09/2020 **STATISTICS (General)**

Time : 11.00 am – 3.00 pm **Paper : II** Full Marks : 50

Group - A

1. Answer **any three** questions : [3×5]

   a) Imagine two vaccines – 1 & 2 are equally effective against Corona Virus. However, there is some suspicion that vaccine 2 causes a serious side effect in some patients, whereas vaccine 1 is being used with no report of side effects. Construct the null & the alternative hypothesis as follows:

   H_0 : The incidence of side-effect in both vaccines is the same.

   H_1 : The incidence of side-effect in vaccine 2 in greater than that in vaccine 1.

   Imagine further that you have only two values of α (i.e. level of significance) to choose from for carrying out above test. The values of α are 0.05 & 0.09. Justify which value of α you would go for. [5]

   b) The upper 0.025 point of t-distribution with 20 degrees of freedom is 2. ie. $P[t_{20} > 2] = 0.025$.From this information, find with suitable justification, the upper 0.05 point of $F_{1,20}$ distribution. [5]

   c) Imagine drawing a random sample $X_1, X_2, \ldots\ldots, X_{16}$ for $N(\mu, \sigma^2 = 2)$.

   Find $P\left[\sum_{i=1}^{16}(X_i - \bar{X})^2 \le 60\right]$ [It is given that $P[\chi^2_{15} \ge 30] = 0.01$. [5]

   d) Let X_1, X_2 be a random sample of size 2 for $N(\mu, \sigma^2)$. Choose, with suitable justification, the best estimator for μ from among the following three estimators: $X_1, X_2 - X_1, X_1 + X_2$. [5]

2. Answer **any two** questions : [2×5]

   a) When would you prefer to use stratified random sampling? Describe with suitable example.

   b) Derive the standard error of the sample mean in case of SRSWR. Show SRSWOR is more efficient than SRSWR.

   c) Write the advantages of sampling over complete enumeration.

Practical

Group : B

1. Answer **any one** question : [1×10]

a) A cold-drink company claims that the content of each its cold-drinks bottle is 300 ml, as advertised. One consumer suspects that the bottles are underfilled. He measures the contents of 10 bottles which are as follows:

299.7	298.1	298.8	297.6	301.1
2971.1	299.3	301.5	300.4	298.3

Test, at 5 % level of significance, if the average content of the bottles is really less than the advertised 300 ml. [Assume that the content of the bottles are normally distributed with a standard deviation 3.5 ml] You're provided $\tau_{0.05} = 1.65$ [10]

b) Let $\bar{X}$ be the mean of a random sample of size n for a distribution that is normal $\left(\mu, \sigma^2 = 9\right)$.

Find n such that $P\left(\bar{X} - 1 < \mu < \bar{x} + 1\right) = 0.90$ (approxly)

[You're provided $\tau_{0.05} = 1.65$] [10]

2. Answer **all** questions :

a) The following table gives the grades of 100 students in mathematics. Draw a random sample of size ten from the group of students with SRSWR and estimate the mean grade from the sample. Also give an estimate of the standard error. [10]

75	58	80	86	76	65	75	76	72	86	83	82	80	88	68
66	63	60	69	80	66	87	73	58	76	74	85	96	60	72
86	79	95	84	41	76	78	74	74	56	50	80	66	96	80
68	79	73	72	73	87	77	60	87	40	82	77	87	76	82
66	81	84	72	63	59	76	52	57	78	79	92	80	65	90
75	74	98	64	45	68	57	79	79	83	35	76	88	67	75
60	52	63	80	94	34	78	64	58	56					

b) Draw a random sample of size 10 from the following data with SRSWOR and estimate the mean from the sample. [5]

45	24	43	17	05	28	27	21	11	46
33	26	24	14	34	21	25	48	35	38
26	27	35	08	30	26	30	28	21	27
20	13	23	36	38	20	25	31	24	18
12									

TABLE VI
RANDOM SAMPLING NUMBERS *

4652	3819	8431	2150	2352	2472	0043	3488
9031	7617	1220	4129	7148	1943	4890	1749
2030	2327	7353	6007	9410	9179	2722	8445
0641	1489	0828	0385	8488	0422	7209	4950
8479	6062	5593	6322	9439	4996	1322	4918
9917	3490	5533	2577	4348	0971	2580	1943
6376	9899	9259	5117	1336	0146	0680	4052
7287	0983	3236	3252	0277	8001	6058	4501
0592	4912	3457	8773	5146	2519	3931	6794
6499	9118	3711	8838	0691	1425	7768	9544
0769	1109	7909	4528	8772	1876	2113	4781
8678	4873	2061	1835	0954	5026	2967	6560
0178	7794	6488	7364	4094	1649	2284	7753
3392	0963	6364	5762	0322	2592	3452	9002
0264	6009	1311	5873	5926	8597	9051	8995
4089	7732	8163	2798	1984	1292	0041	2500
9376	7365	7987	1937	2251	3411	6737	0367
3039	3780	2137	7641	4030	1604	2517	9211
8971	8653	1855	5285	5631	2649	6696	5475
0373	4153	5199	5765	2067	6627	3100	5716
9092	4773	0002	7000	7800	2292	2933	6125
2464	1038	3163	3569	7155	2029	2538	7080
3027	6215	3125	5856	9543	3660	0255	5544
5754	9247	1164	3283	1865	5274	5471	1346
4358	3716	6949	8502	1573	5763	5046	7135
7178	8324	8379	7365	4577	4864	0629	5100
5035	5939	3665	2160	6700	7249	1738	2721
3318	0220	3611	9887	4608	8664	2185	7290
9058	1735	7435	6822	6622	8286	8901	5534
7886	5182	7595	0305	4903	3306	8088	3899
3354	8454	7386	1333	5345	6565	3159	3991
3415	7671	0846	7100	1790	9449	6285	2525
3918	5872	7898	6125	2268	1898	0755	6034
6138	9045	6950	8843	6533	0917	6673	5721
3825	1704	2835	4677	4637	7329	3156	3291
1349	0417	9311	9787	1284	0769	8422	1077
4234	0248	7760	6504	2754	4044	0842	9080
6880	3201	7044	3657	5263	0374	7563	6599
0714	5008	5076	1134	5342	1608	5179	0967
3448	6421	3304	0583	1260	0662	7257	0766
5711	7343	7539	3684	9397	5335	4031	1486
2588	3301	0553	2427	3598	2580	7017	9176
8581	4253	7404	5264	5411	3431	3092	8573
8475	6322	3949	9675	6533	1133	8776	2216
0272	5624	8549	5552	7469	2799	2822	9620
7383	7795	7939	2652	4456	6993	2950	8573
5126	2089	7729	0945	3901	4445	7117	8186
2064	3760	0939	7319	5939	3432	2030	4752
9315	8185	7805	6294	7072	6491	4012	1016
6814	8752	3462	6001	3302	3895	7371	3432

———— × ————